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Abstract

Program slicing, introduced by Weiser, is known to help programmers in understanding foreign code and in debugging. We apply program slicing to the maintenance problem by extending the notion of a program slice (that originally required both a variable and line number) to a decomposition slice, one that captures all computation on a given variable; i.e., is independent of line numbers. Using the lattice of single variable decomposition slices, ordered by set inclusion, we demonstrate how to form a slice-based decomposition for programs. We are then able to delineate the effects of a proposed change by isolating those effects in a single component of the decomposition. This gives maintainers a straightforward technique for determining those statements and variables that may be modied in a component and those that may not. Using the decomposition, we provide a set of principles to prohibit changes that will interfere with unmodied components. These semantically consistent changes can then be merged back into the original program in linear time. Moreover, the maintainer can test the changes in the component with the assurance that there are no linkages into other components. Thus, decomposition slicing induces a new software maintenance process model that eliminates the need for regression testing.

Index terms: Software Maintenance, Program Slicing, Decomposition Slicing, Software Process Models Software Testing, Software Tools, Impact Analysis

1 Introduction

In "Kill that Code!," [32] Gerald Weinberg alludes to his private list of the world's most expensive program errors. The top three disasters were caused by a change to exactly one line of code: \each one involved the change of a single digit in a previously correct program." The argument goes that since the change was to only one line, the usual mechanisms for change control could be circumvented. And, of course, the results were catastrophic. Weinberg offers a partial explanation: "unexpected linkages," i.e., the value of the modied variable was used in some other place in the program. The top three of this list of ignominy are attributed to linkage. More recently, in a special section of the March, 1987 issue of IEEE Transactions on Software Engineering, Schneidewind [30] notes that one of the reasons that maintenance is difficult is that it is hard to determine when a code change will affect some other piece of code. We present herein a method for maintainers to use that addresses this issue.

While some may view software maintenance as a less intellectually demanding activity than development, the central premise of this work is that software maintenance is more demanding. The added difficulty is due in large part to the semantic constraints that are placed on the maintainer. These constraints can be loosely characterized as the attempt to avoid unexpected linkages. Some [4, 14] have addressed this problem by attempting to eliminate these semantic constraints and then providing the maintainer with a tool that will pinpoint potential inconsistencies after changes have been implemented. This makes maintenance appear to be more like development, since the programmer does not need to worry about linkages: once the change is made, the tool is invoked and the inconsistencies (if any) are located. One would expect that the tool would proceed to resolve these inconsistencies, but it has been shown that this problem is NP-hard [14]. Thus, the maintainer can be presented with a problem that is more difficult to resolve that the original change.

We take the opposite view: present the maintainer with a semantically constrained problem and let him construct the solution that implements the change within these constraints. The semantic context with which we propose to constrain the maintainer is one that will *prohibit* linkages into the portions of the code that the maintainer does not want to change. This approach uncovers potential problems earlier than the aforementioned methods, and, we believe, is worth any inconvenience that may be encountered due to the imposition of the constraints.

Our program slicing based techniques give an assessment of the impact of proposed modifications, ease the problems associated with revalidation and reduce the resources required for maintenance activities. They work on unstructured programs, so they are usable on older systems. They may be used for white-box, spare-parts and backbone maintenance without regard to whether the maintenance is corrective, adaptive, perfective or preventive.

2 Background

Program slicing, introduced by Weiser, [33, 36] is a technique for restricting the behavior of a program to some specified subset of interest. A slice $S(v, n)$ (of program P) on variable v, or set of variables, at statement n yields the portions of the program that contributed to the value of v just before statement n is executed. $S(v, n)$ is called a *slicing criteria*. Slices can be computed automatically on source programs by analyzing data flow and control flow. A program slice has the added advantage of being an executable program. Slicing is done implicitly by programmers while debugging [33, 35]; slices can be combined to isolate sections of code likely to contain program faults and signicantly reduce debugging times [23, 24, 25].

There has been a flurry of recent activities where slicing plays a significant role. Horwitz, Reps, et al. [15, 16, 28] use slices in integrating programs. Their results are built on the seminal work of Ottenstein and Ottenstein $[7, 27]$ combining slicing with the robust representation afforded by program dependence graphs. Korel and Laski [20, 21, 22] use slices combined with execution traces for program debugging and testing. Choi et al. [6] use slices and traces in debugging parallel programs. Reps and Wang [29] have investigated termination conditions for program slices. Hausler [13] has developed a denotational approach to program slicing. Gallagher [8] has improved Lyle's [23] algorithm for slicing in the presence of GOTO's and developed techniques for capturing arbitrarily placed output statements. We will not discuss slicing techniques in this paper and instead refer the interested reader to these works.

Since we want to avoid getting bogged down in the details of a particular language, we will identify a program with its flowgraph. Each node in the graph will correspond to a single source language statement.


```
 #define YES 1
12 #define NO 0
3 main()
4\left\{ \right.5 int c, nl, nw, nc, inword ;
6 inword = NO ;
7nl = 0;8nw = 0;\mathbf{Q}nc = 0;
10c = getchar();
11while ( c != EOF ) {
12nc = nc + 1;
                        if ( c == ' \n\langle n' \rangle1314nl = nl + 1;if ( c == '' ' || c == '\n' || c == '\t')
1516 inword = NO;
17else if (inword == NO) {
18 inword = YES ;
19
                                nw = nw + 1;
20-general control of the control of t
2.1c = getchar();
- -
22graduate and the contract of the
23printf("%d \n",nl);
24printf("%d \n",nw);
- -
25 printf("%d \n",nc);
        \mathcal{E}26
```
Figure 1: Program to be Sliced

Henceforth, the term statement will mean a node in the flowgraph. Using a common representation scheme makes the presentation clear, although it is clear that any tool based on these techniques will need to account for the nuances of the particular language. In this paper, we also ignore problems introduced by having dead code in the source program, and declare that the programs under consideration will not have any dead code. See [8] for slicing based techniques to eliminate dead code.

Figures 2-6 illustrate slicing on the program of figure 1, a bare bones version of the Unix utility wc , word count, taken from [19]. The program counts the number of characters, words, and lines in a text file. It has been slightly modified to illustrate more clearly the slicing principles. The slices of figures 2-4 are complete programs that compute a restriction of the specification. The slice on nw (fig. 2) will output the number of words in a file; the slice on **nc** (fig. 3) will count the number of characters in the input text file; the slice on \mathbf{n} l (fig. 4) will count the number of lines in the file.

3 Using Slices for Decomposition

This section presents a method for using slices to obtain a decomposition of the program. Our objective is to use slicing to decompose a program \directly," into two (or more) components. A program slice will be one of the components. The construction is a two step process. The first step is to build, for one variable, a decomposition slice, which is the union of certain slices taken at certain line numbers, on the given variable. Then the other component of the decomposition, called the \complement," will also be obtained from the original program. The complement is constructed in such a way that when certain statements of the decomposition slice are removed from the original program, the program that remains is the slice that


```
1 #define YES 1
2 #define NO 0
3 main()
4 f
5 int c, nw, inword ;
6 inword = NO ;
8nw = 0;10c = getchar();
11while ( c != EOF ) {
15if ( c == '' ' || c == '\n' || c == '\t')
16 inword = NO;
17else if (inword == NO) {
18 inword = YES ;
19nw = nw + 1;general control of the control of t
21c = getchar();
22\}24printf("%d \n\t\frac{\nu}{\mu}, nw);
26\mathcal{F}
```
Figure 2: Slice on (nw,26): Word Counter

```
3 main()
4\{5<sup>1</sup> int c, nc ;
9nc = 0;
10c = getchar();
11while ( c != EOF ) {
12nc = nc + 1;21c = getchar();
22\}25printf("%d \infty",nc);
     \}26
```
Figure 3: Slice on (nc,26): Character Counter


```
3 main()
4 f
5<sup>5</sup> int c, nl, ;
7 nl = 0;
10c = getchar();
11while ( c != EOF ) {
13if ( c == ' \n\times)
                     nl = nl + 1;1421c = getchar();
22\}23printf("%d \n",nl);
26\}
```
Figure 4: Slice on (nl,26): Line Counter

```
1 #define YES 1
2 #define NO 0
3 main()
4 f
5 int c, inword ;
6 inword = NO ;
10c = getchar();
11while ( c != EOF ) {
15if ( c == ' ' || c == '\n' || c == '\t')
16 inword = NO;
17else if (inword == NO) {
18 inword = YES ;
20general control of the control of t
21c = getchar();
22\}26\}
```
Figure 5: Slice on (inword,26)

```
3 main()
4 f
5 int c ;
10c = getchar();
11while ( c != EOF ) {
21c = getchar();
22\}26\}
```
Figure 6: Slice on (c,26)

Figure 7: Requires a Decomposition Slice

corresponds to the *complement* (in a sense to be defined) of the given criteria, with respect to the variables defined in the program. Thus the complement is also a program slice.

The decomposition slice is used to guide the removal of statements in a systematic fashion to construct the complement. It is insufficient to merely remove the slice statements from the original program. Since we require that a slice be executable, there will be certain crucial statements that are necessary in both the slice and its complement. For example, if we start with the slice of figure 2 and remove all its statements from the original program, the resulting object will not even compile!

We use this decomposition to break the program into manageable pieces and automatically assist the maintainer in guaranteeing that there are no ripple effects induced by modifications in a component. We use the complement to provide a semantic context for modications in the decomposition slice; the complement must remain xed after any change.

The decomposition ideas presented in this section are independent of a particular slicing method. Once a slice is obtained, by any slicing algorithm, a program decomposition may be computed. Clearly, the quality of the decomposition will be affected by the quality of the slice, in the sense that more refined slices give a finer granularity and also deliver more semantic information to the maintainer.

A program slice is dependent on a variable and a statement number. A decomposition slice does not depend on statement numbers. The motivation for this concept is easily explained using the example of figure 7. The slice $S(t,4)$ is statements 1, 2, 3, 4, while the slice $S(t,6)$ is statements 1, 2, 5, 6. Slicing at statement *last* (in this case 6) of a program is insufficient to get all computations involving the slice variable, t. A decomposition slice captures all relevant computations involving a given variable.

To construct a decomposition slice, we borrow the concept of critical instructions from an algorithm for dead code elimination as presented in Kennedy [18]. A brief reprise follows. The usual method for dead code elimination is to first locate all instructions that are useful in some sense. These are declared to be the critical instructions. Typically, dead code elimination algorithms start by marking output instructions to be critical. Then the use-definition [18] chains are traced to mark the instructions that impact the output statements. Any code that is left unmarked is useless to the given computation.

Definition 1 Let Output (P, v) be the set of statements in program P that output variable v, let last be the last statement of P, and let $N = Output(P, v) \cup \{last\}$. The statements in $|| \cdot ||$ n *n* 1 s () *form the decomposition*

slice on v , denoted $S(v)$.

The decomposition slice is the union of a collection of slices, which is still a program slice [36]. We include statement last so that a variable that is not output may still be used as a decomposition criteria; this will also capture any defining computation on the decomposition variable after the last statement that displays its value. To successfully take a slice at statement last, we invoke one of the crucial differences between the slicing definitions of Reps, with those of Weiser, Lyle and this work. A Reps slice must be taken at a point, p , with respect to a variable that is defined or referenced at p . Weiser's slices can be taken at an arbitrary variable at an arbitrary line number. This difference prohibits Reps' slicing techniques from being applicable in the current context, since we want to slice on every variable in the program at the last statement.

We now begin to examine the relationship between decomposition slices. Once we have this in place, we can use the decomposition slices to perform the actual decompositions. To determine the relationships, we take the decomposition slice for each variable in the program and form a lattice of these decomposition slices,

ordered by set inclusion. It is easier to gain a clear understanding of the relationship between decomposition slices if we regard them without output statements. This may seem unusual in light of the above definition, since we used output statements in obtaining relevant computations. We view output statements as windows into the current state of computation, which do not contribute to the realization of the state. This coincides with the informal definition of a slice: the statements that yield the portions of the program that contributed to the value of v just before statement n is executed. Assuming that output statements do not contribute to the value of a variable precludes from our discussion output statements (and therefore programs) in which the output values are reused, as is the case with random access files or output to files that are later reopened for input. Moreover, we are describing a decomposition technique that is not dependent on any particular slicing technique; we have no way of knowing whether or not the slicing technique includes output statements or not. We say a slice is output-restricted if all its output statements are removed.

Definition 2 Output restricted decomposition slices $S(v)$ and $S(w)$ are independent if $S(v) \cap S(w) = \emptyset.$

It would be a peculiar program that had independent decomposition slices; they would share neither control flow or data flow. In effect, there would be two programs with non-intersecting computations on disjoint domains that were merged together. The lattice would have two components. In Ott's slice metric terminology, [26] independence corresponds to low (coincidental or temporal) cohesion.

Output-restricted decomposition slices that are not independent are said to be (weakly) dependent. Subsequently, when we speak of independence and dependence of slices it will always be in the context of output-restricted decomposition slices.

Definition 3 Let $S(v)$ and $S(w)$ be output-restricted decomposition slices, $w \neq v$, and let $S(v) \subset S(w)$. $S(v)$ is said to be strongly dependent on $S(w)$.

Thus output-restricted decomposition slices strongly dependent on independent slices are independent. The definitions of independence and dependence presented herein are themselves dependent on the notion of a slice.

The analogous definitions are used by Bergeretti and Carré [3] to $define$ slices. In Ott's metric terminology, [26] strong dependence corresponds to high (sequential or functional) cohesion.

Strong dependence of decomposition slices is a binary relation; in most cases, however, we will not always need an explicit reference to the containing slice. Henceforth, we will write $\mathscr{S}(v)$ is strongly dependent" as a shorthand for " $S(v)$ is strongly dependent on some other slice $S(w)$ " when the context permits it.

Definition 4 An output-restricted slice $S(v)$ that is not strongly dependent on any other slice is said to be maximal.

Maximal decomposition slices are at the "ends" of the lattice. This definition gives the motivation for output restriction; we do not want to be concerned with the possible effects of output statements on the maximality of slices or decomposition slices. This can be observed by considering the decomposition slices on nw and inword, of figures 2 and 5. If we regarded output statements in defining maximal, we could force the slice on **inword** to be maximal by the addition of a *print* statement referencing **inword** along with the others at the end of the program. Such a statement would not be collected into the slice on nw. Since this added statement is not in any other slice, the slice on inword would be maximal and it should not be.

Figure 8 gives the lattice we desire. $S(nc)$, $S(nl)$ and $S(nw)$ are the maximal decomposition slices. $S(nword)$ is strongly dependent on $S(nw)$; $S(c)$ is strongly dependent on all the other decomposition slices. The decomposition slices on $S(nw)$, $S(nc)$, and $S(nl)$, figures 2 - 4 they are weakly dependent and maximal, when the output statements are removed. There are no independent decomposition slices in the example. Recall that independent decomposition slices cannot share any control flow: the surrounding control statements would make them dependent.

We now begin to classify the individual statements in decomposition slices.

Definition 5 Let $S(v)$ and $S(w)$ be output-restricted decomposition slices of program P. Statements in $S(v) \cap S(w)$ are called slice dependent statements.

Figure 8: Lattice of Decomposition Slices.

Slice independent statements are statements that are not slice dependent. We will refer to slice dependent statements and slice independent statements as dependent statements and independent statements. Dependent statements are those contained in decomposition slices that are interior points of the lattice; independent statements are those in a maximal decomposition slice that are not in the union of the decomposition slices that are properly contained in the maximal slice. The terms arise from the fact that two or more slices depend on the computation performed by dependent statements. Independent statements do not contribute to the computation of any other slice. When modifying a program, dependent statements cannot be changed, or the effect will ripple out of the focus of interest.

For example, statement 12 of the slice on \mathbf{nc} (fig. 3) is a slice independent statement with respect to any other decomposition slice. Statements 13 and 14 of the slice on \mathbf{n} (fig. 4) are also slice independent statements with respect to any other decomposition slice. The decomposition slice on c (fig. 6) is strongly dependent on all the other slices, thus all its statements are slice dependent statements with respect to any other decomposition slice. Statements 6 and 15-20 of the slice on \bf{nw} (fig. 2) are slice independent statements with respect to decomposition slices $S(nc)$, $S(nl)$, and $S(c)$; only statement 19 is slice independent when compared with $S(nword)$. Statements 6, 15-18 and 20 of the decomposition slice on **inword** (fig. 5) are slice independent statements with respect to decomposition slices $S(nc)$, $S(nl)$, and $S(c)$; no statements are slice independent when compared with $S(nw)$.

We have a relationship between maximal slices and independent statements. This proposition permits us to apply the terms "(slice) independent statement" and "(slice) dependent statement" in a sensible way to a particular statement in a given maximal decomposition slice without reference to the binary relation between decomposition slices that is required in definition 5.

Proposition 1 Let

- 1. Varset(P) be the set of variables in program P.
- 2. $S(v)$ be an output-restricted decomposition slice of P.
- 3. Let $M = \{ m \in Varset(P) \mid S(m) \text{ is maximal} \}$
- 4. Let $U = M \{ v \}$

The statements in S(v) . . \sim S(u) are independent.

Proof Sketch: Let ^U = fu1; . . . ; umg. \sim \sim \sim \sim \sim \sim \sim S(u) = S(v) S(u1) . . . S(um).

There is a relationship between the maximal slices and the program. (Recall that dead code has been excluded from our discussions.)

Proposition 2 Let
$$
M = \{ m \in Varset(P) | S(m) \text{ is maximal} \}
$$
. Then $\bigcup_{m \in M} S(m) = P$.

Proof Sketch:

Since $S(m) \in P$, $\cup_{m\in M}S(m) \subset P$. If $P \not\subseteq \cup_{m\in M}S(m)$, then the statements in P that are not in $\cup_{m\in M}S(m)$ are dead code.

End.

Maximal slices capture the computation performed by the program. Maximal slices and their respective independent statements also are related:

Proposition 3 An output-restricted decomposition slice is maximal iff it has at least one independent statement.

Proof Sketch:

Suppose $S(v)$ is maximal. By definition $S(v)$ has at least one statement that no other slice has. This statement is an independent statement.

Now suppose that $S(v)$ has an independent statement, s. Then s is not in any other slice, and the slice that contains ^s is maximal.

End.

Conversely, a slice with no independent statements is strongly dependent.

We also have another characterization of strongly dependent slices.

Proposition 4 Let

1. Varset(P) be the set of variables in program P.

2. $S(v)$ be an output-restricted decomposition slice of P.

- 3. Let $D = \{ w \in Varset(P) \mid S(v) \text{ is strongly dependent on } S(w) \}$
- 4. Let $M = \{ m \in Varset(P) \mid S(m) \text{ is maximal} \}$

5. Let
$$
U = M - \{ v \}
$$

An output-restricted decomposition slice $S(v)$ is strongly dependent (on some $S(d)$) iff \Box u2U S(u) = ^P .

Proof Sketch:

Suppose $S(v)$ is strongly dependent. We need to show that D has a maximal slice. Partially order D by set inclusion. Let d be one of the maximal elements of D. The element d is maximal; if it is not, then it is properly contained in another slice d_1 , which is in D and contains $S(v)$. Then $d \in M$, $d \neq v$, and $S(v)$ makes no contribution to the union.

Suppose $\bigcup S(u) = P$. Since $U \subset M$, $S(v)$ makes no contribution to the union. By proposition 3, $S(v)$ $u \in U$

is strongly dependent.

End.

We are now in a position to state the decomposition principles. Given a maximal output-restricted decomposition slice $S(v)$ of program P, delete the independent and output statements of S from P. We will denote this program $\sum(v)$ and call it the *complement of decomposition slice* $S(v)$ (with respect to P). Henceforth, when we speak of complements, it will always be in the context of decomposition slices. The decomposition slice is the subset of the program that computes a subset of the specification; the complement computes the rest of the specification.

Figures 9 - 11 give the complements of the slices on \bf{nw} , \bf{nc} and \bf{n} of figures 2 - 4. Using proposition 4 we obtain that the complement of both the slice on **inword** and the slice on c is the entire program.


```
3 main()
4 f
5 int c, nl, nw, nc, inword ;
7nl = 0;9
                  nc = 0;\overline{\phantom{a}}c = getchar();
10
-111while ( c != EOF ) {
                            nc = nc + 1;1213if ( c == ' \n\langle n' \rangle14
                                     nl = nl + 1;
21c = getchar();
22graduate and the contract of the
                  printf("%d \n\t\frac{\nu}{n}, n1);
23
25
                  printf("%d \n\t\frac{\nu}{\alpha},nc);
         \mathcal{E}26
```
Figure 9: $\sum(nw)$. Complement of slice on **nw**: computes line count and character count

This yields the approximation of a direct sum decomposition of a program that preserves the computational integrity of the constituent parts. This also indicates that the only useful decompositions are done with maximal decomposition slices. A complement, Σ , of a maximal slice can be further decomposed, so the decomposition may be continued until all slices with independent statements (i.e. the maximal ones) are obtained.

In practice, a maintainer may find a strongly dependent slice as a starting point for a proposed change. Our method will permit such changes. Such a change may be viewed as properly *extending* the domain of the partial function that the program computes, while preserving the partial function on its original domain.

$\overline{4}$ 4 Application to Modication and Testing

Statement independence can be used to build a set of guidelines for software modication. To do this, we need to make one more set of definitions regarding variables that appear in independent and dependent statements. With these definitions we give a set of rules that maintainers must obey in order to make modifications without ripple effects and unexpected linkages. When these rules are obeyed, we have an algorithm to merge the modified slice back into the complement and effect a change. The driving motivation for the following development is: "What restrictions must be placed on modifications in a decomposition slice so that the *complement* remains intact?"

Definition 6 A variable that is the target of a dependent assignment statement is called a dependent variable. Alternatively, and equivalently, if all assignments to a variable are in independent statements, then the variable is called an independent variable.

An assignment statement can be an independent statement while its target is not an independent variable. In the program of figure 12 the two maximal decomposition slices are $S(a)$ and $S(e)$ (figures 13 and 14). Slice $S(b)$ (figure 15) is strongly dependent on $S(a)$ and $S(f)$ (figure 16) is strongly dependent on $S(b)$ and $S(a)$. S(d) and S(c) (not shown) are strongly dependent on both maximal slices. In S(a), statements 8, 10, and 11 are independent, by the proposition. But *variables* a and **b** are targets of assignment statements 6 and 5, respectively. So, in the decomposition slice $S(a)$, only variable f is an independent variable.


```
1 #define YES 1
2 #define NO 0
3 main()
4 f
5 int c, nl, nw, nc, inword ;
6 inword = NO ;
7 nl = 0;
8 nw = 0;
9nc = 0;10c = getchar();
11while ( c != EOF ) {
12nc = nc + 1;13if ( c == ' \n\times)
14nl = nl + 1;15if ( c == '' ' || c == '\n' || c == '\t')
16 inword = NO;
17else if (inword == NO) {
18 inword = YES ;
19nw = nw + 1;
20general control of the control of t
21c = getchar();
22\}23printf("%d \n",nl);
24printf("%d \n",nw);
26\}
```
Figure 10: \sum (*nc*). Complement of slice on **nc**: computes word count and line count


```
1 #define YES 1
2 #define NO 0
3 main()
4 f
5 int c, nl, nw, nc, inword ;
6 inword = NO ;
8nw = 0;9nc = 0;10c = getchar();
11while ( c != EOF ) {
12nc = nc + 1;
15if ( c == '' ' || c == '\n' || c == '\t')
16 inword = NO;
17else if (inword == NO) {
18 inword = YES ;
19nw = nw + 1;20general control of the control of th
21c = getchar();
22\}24printf("%d \n\t\frac{\nu}{\sqrt{d}}, nw);
25 printf("%d \n",nc);
26\}
```
Figure 11: $\sum_{i=1}^{\infty}$. Complement of slice on nl: computes character count and word count

```
1 main()
\overline{2}\{3 int a, b, c, d, e, f;
4c = 4;b = c;5a = b + c;
67d = a + c;8f = d + b;9e = d + 8;
     b = 30 + f;
1011a = b + c;
-1
```
Figure 12: Dependent Variable Sample Program


```
1 main()
- - -3 int a, b, c, d, e, f;
4c = 4;5b = c;6a = b + c;
7d = a + c;8f = d + b;10 b = 30 + f;
11a = b + c;
```
 -1

Figure 13: Slice on ^a

```
1 main()
- - -3 int a, b, c, d, e, f;
4c = 4;5b = c;6a = b + c;
7d = a + c;9e = d + 8;
-1
```
Figure 14: Slice on ^e


```
 main()
12 f
3 int a, b, c, d, e, f;
4c = 4;
5b = c;6a = b + c;
7d = a + c;8f = d + b;10b = 30 + f;
12 }
```
graduate and the contract of the contract of

 -1

Figure 15: Slice on ^b

```
1 main()
2 f
3 int a, b, c, d, e, f;
4c = 4;5b = c;6a = b + c;
7d = a + c;8f = d + b;
```
Figure 16: Slice on ^f

A similar argument applies for independent control flow statements that reference dependent variables. A dependent variable in an independent statement corresponds to the situation where the variable in question is required for the compilation of the complement, but the statement in question does not contribute to the complement. If a variable is referenced in a dependent statement, it is necessary to the complement and cannot be independent.

If a decomposing on a single variable yields a strongly dependent slice, we are able to construct a slice where the original slice *variable* is an independent variable.

Proposition 5 Let

- 1. Varset(P) be the set of variables in program P.
- 2. $S(v)$ be a strongly dependent output restricted decomposition slice of P.
- 3. Let $D = \{ w \in Varset(P) \mid S(v) \text{ is strongly dependent on } S(w) \}$
- 4. Let $M = \{ m \in Varset(P) \mid S(m) \text{ is maximal} \}$
- 5. Let $U = D \cap M$
- 6. Let $T = \vert \vert$ u2U

The variable ^v is an independent variable in ^T .

In other words, when $S(v)$ is a strongly dependent slice and T is the union of all the maximal slices upon which $S(v)$ is strongly dependent, then v is an independent variable in T.

Proof Sketch:

We show that the complement of T, P - T has no references to v: if variable v is in the complement of T, then there is a maximal slice in the complement upon which $S(v)$ is strongly dependent. This contradicts the hypotheses, so the complement if T has no references to v and the variable v is independent in T .

End.

This can be interpreted as the variable version of proposition 1, that refers to statements.

This has not addressed the problem that is presented when the decomposition slice on variable is maximal, but the variable itself remains dependent. This is the situation that occurred in the example at the beginning of the chapter; the slice on variable a (figure 13) is maximal but the variable is dependent. The solution is straightforward: we construct the slice that is the union of all slices in which the the variable is dependent.

Proposition 6 Let

1. Varset(P) be the set of variables in program P.

- 2. $S(v)$ be an output restricted decomposition slice of P.
- 3. Let $E = \{ w \in Varset(P) \mid v \text{ is a dependent variable in } S(w) \}$

4. Let $T = \Box$ -1

We have two cases:

1. $E = \emptyset$, (and thus T is empty also) in which case v is an independent variable.

2. $E \neq \emptyset$, so T is not empty and the variable v is an independent variable in T.

Proof Sketch:

Case 1: $E = \emptyset$

 $S(v)$ contains all references to v. In particular, $S(v)$ contains all assignments to v. So v is an independent variable in $S(v)$. End Case 1

Case 2: $E \neq \emptyset$

T contains all references to v. In particular, T contains all assignments to v. So v is an independent variable in T. End Case 2

 $End.$

This proposition is about *variables*.

4.1Modifying Decomposition Slices

We are now in a position to answer the question posed at the beginning of this section. We present the restrictions as a collection of rules with justications.

Modications take three forms: additions, deletions and changes. A change may be viewed as a deletion followed by an addition. We will use this second approach, and determine only those statements in a decomposition slice that can be deleted and the forms of statements that can be added. Again, we must rely on the fact that the union of decomposition slices is a slice, since the complementary criteria will usually involve more than one maximal variable. We also assume that the maintainer has kept the modified program compilable and has obtained the decomposition slice of the portion of the software that needs to be changed. (Locating the code may be a highly nontrivial activity; for the sake of the current discussion, we assume its completion.)

Since independent statements do not affect data flow or control flow in the complement, we have:

Rule 1 Independent statements may be deleted from a decomposition slice.

Reason:

Independent statements do not affect the computations of the complement. Deleting an independent statement from a slice will have no impact on the complement.

End.

This result applies to control flow statements and assignment statements. The statement may be deleted even if it is an assignment statement that targets a dependent variable, or a control statement that references a dependent variable. The point to keep in mind is that if the statement is independent it does not affect the complement. If an independent statement is deleted, there will certainly be an effect in the slice. But the purpose of this methodology is to keep the complement intact.

There are a number of situations to consider when statements are to be added. We progress from simple to complex. Also note that for additions, new variables may be introduced, as long as the variable name does not clash with any name in the complement. In this instance the new variable is independent in the decomposition slice. In the following, *independent variable* means an independent variable or a new variable.

Rule 2 Assignment statements that target independent variables may be added anywhere in a decomposition slice.

Reason :

Independent variables are unknown to the complement. Thus changes to them cannot affect the computations of the complement.

End.

This type of change is permissible even if the changed value flows into a dependent variable. In figure 13, changes are permitted to the assignment statement a line 8 , which targets \mathbf{f} . A change here would propagate into the values of dependent variables ^a and ^b at lines 10 and 11. The maintainer would then be responsible for the changes that would occur to these variables. If lines 10 and 11 were dependent, (i.e., contained in another decomposition slice), line 8 would also be contained in this slice, and variable ^f would be dependent.

Adding control flow statements requires a little more care. This is required because control statements have two parts: the logical expression, that determines the flow of control, and the actions taken for each value of the expression. (We assume no side effects in the evaluation of logical expressions.) We discuss only the addition of if-then-else and while statements, since all other language constructs can be realized by them [5].

Rule 3 Logical expressions (and output statements) may be added anywhere in a decomposition slice.

Reason :

We can inspect the state of the computation anywhere. Evaluation of logical expressions (or the inclusion of an output statement) will not even affect the computation of the slice. Thus the complement remains intact.

End.

We must guarantee that the statements that are controlled by newly added control flow do not interfere with the complement.

Rule 4 New control statements that surround (i.e. control) any dependent statement will cause the complement to change.

Reason :

Suppose newly added code controls a dependent statement.

Let C be the criteria that yield the complement. When using this criteria on the modified program, the newly added control code will be included in this complementary slice. This is due to the fact that the dependent statements are in both the slice and the complement. Thus any control statements that control dependent statements will also be in the slice and the complement.

End.

By making such a change, we have violated out principle that the complement remain fixed. Thus new control statements may not surround any dependent statement.

This short list is necessary and sufficient to keep the slice complement intact. This also has an impact on testing the change that will be discussed later.

Changes may be required to computations involving a dependent variable, v, in the extracted slice. The maintainer can choose one of the following two approaches:

1. Use the techniques of the previous section to extend the slice so that \bf{v} is independent in the slice.

2. Add a new local variable (to the slice), copy the value to the new variable, and manipulate the new name only. Of course, the new name must not clash with any name in the complement. This technique may also be used if the slice has no independent statements, i.e., it is strongly dependent.

Merging the Modications into the Complement 4.2

Merging the modied slice back into the complement is straightforward. A key to understanding the merge operation comes the the observation that through the technique, the maintainer is editing the entire program. The method gives a view of the program with the unneeded statements deleted and with the dependent statements restricted from modification. The slice gives smaller piece of code for the maintainer to focus on, while the rules of the previous subsection provide the means by which the deleted and restricted parts cannot be changed accidentally.

We now present the merge algorithm.

- 1. Order the statements in the original program. (In the following examples, we have one statement per line so that the ordering is merely the line numbering.) A program slice and its complement can now be identified with the subsequence of statement numbers from original program. We call the sequence numbering from the slice, the *slice sequence* and the numbering of the complement the *complement* sequence. We now view the editing process as the addition and deletion of the associated sequence numbers.
- 2. For deleted statements, delete the sequence number from the slice sequence. Observe that since only independent statements are deleted, this number is not in the complement sequence.
- 3. For statements inserted into the slice a new sequence number needs to be generated. Let ^P be the sequence number of the statement preceding the statement to be inserted. Let ^M be the least value in the slice sequence greater than P. Let $F = min(int(P + 1), M)$. Insert the new statement at sequence number $(F + P)/2$. (Although this works in principle, in practice, more care needs to be taken in the generation of the insertion sequence numbers to avoid floating point errors after 10 inserts.)
- 4. The merged program is obtained by merging the modied slice sequence values (i.e. statements) into the complement sequence.

Thus, the unchanged dependent statements are used to guide the reconstruction of the modified program. The placement of the changed statements within a given control flow is arbitrary. Again, this becomes clearer when the editing process is viewed as modication to the entire program. The following example will help clarify this.

4.3Testing the Change

Since the maintainer must restrict all changes to independent or newly created variables testing is reduced to testing the modied slice. Thus the need for regression testing in the complement is eliminated. There are two alternative approaches to verifying that only the change needs testing. The first is to slice on the original criteria plus any new variables minus any eliminated variables. and compare its complement with the complement of the original: they should match exactly. The second approach is to preserve the criteria that produced the original complement. Slicing out on this must produce the modified slice exactly.

An axiomatic consideration illumines this idea. The slice and its complement perform a subset of the computation; where the computations meet are the dependencies. Modifying code in the independent part of the slice, leaves the independent part of the complement as an invariant of the slice (and vice versa).

If the required change is "merely" a module replacement, the preceding techniques are still applicable. The slice will provide a harness for the replaced module. A complete independent program supporting the module is obtained. One of the principle benefits of slicing is highlighted in this context: any side effects of the module to be replaced will also be in the slice. Thus the full impact of change is brought to the attention of the modifier.

As an example, we make some changes to $S(nw)$, the slice on **nw**, the word counter of figure 2. The changed slice is shown in figure 17. The original program determined a word to be any string of "nonwhite" symbols terminated by a "white" symbol (space, tab, or newline). The modification changes this


```
3 main()
4 f
* int ch;
5 int c, nw ;
\astch = 0;8nw = 0;10 c = getchar();
                  while ( c != EOF ) {
11-1 if (isspace(c) && isalpha(ch))
\ast\astnw = nw + 1;
\astch = c ;
\overline{21}c = getchar();
22
    graduate and the contract of the
24
                  printf("%d \n\t\frac{\nu}{\mu}, nw);
         \}26
```
Figure 17: Modied slice on nw, the word counter

to requirement to be alphabetical characters terminated by white space. (The example is illustrating a change, not advocating it.) Note the changes. We have deleted the independent \variables" YES and NO; added a new, totally independent variable ch, and revamped the independent statements. The addition of the C macros isspace and isalpha is safe, since the results are only referenced. We test this program independently of the complement.

Figure 18 shows the reconstructed, modified program. Taking the decomposition slice on nw generates the program of figure 17. Its complement is already given in figure 9. The starred $(*)$ statements indicate where the new statements would be placed using the line number generation technique above.

5 A New Software Maintenance Process Model

The usual Software Maintenance Process Model is depicted in figure 19. A request for change arrives. It may be adaptive, perfective, corrective, or preventive. In making the change, we wish to minimize defects, effort, and cost, while maximizing customer satisfaction [12]. The software is changed, subject to pending priorities. The change is composed of two parts. Understanding the code, which may require documentation, code reading, and execution. Then the program is modified. The maintainer must first design the change (which may be subject to peer review) then alter the code itself, while trying to minimize side effects. The change is then validated. The altered code itself is verified to assure conformance with the specification. Then the new code is integrated with the existing system to insure conformance with the system specications. This task involves regression testing.

The new model is depicted in figure 20. The software is changed, subject to pending priorities. The change is composed of two parts. Understanding the code will now require documentation, code reading, execution, and the use of decomposition slices. The decomposition slices may be read, and executed (a decided advantage of having executable program slices). The code is then modified, subject to the strictures outlined. Using those guidelines, no side effects or unintended linkages can be induced in the code, even by accident. This lifts a substantial burden from the maintainer.

The change is tested in the decomposition slice. Since the change cannot ripple out into other modules, regression testing is unnecessary. The maintainer need only verify that change is correct. After applying the merge algorithm, the change (of the code) is complete.


```
3 main()
4 f
* int ch;
5 int c, nl, nw, nc ;
\astch = 0;7nl = 0;8nw = 0;9nc = 0;10c = getchar();
11while ( c != EOF ) {
\ast if (isspace(c) && isalpha(ch))
\astnw = nw + 1;
\astch = c;
12nc = nc + 1;13if ( c == \langle n' \rangle)
14nl = nl + 1;21c = getchar();
             \mathcal{E}2223printf("%d \n",nl);
2.4printf("%d \n\t\frac{\nu}{\alpha} \n\t\frac{\nu}{\gamma};
- -
25printf("%d \n\t\frac{\nu}{\alpha},nc);
      \}26
```
Figure 18: Modied Program

6 Future Directions

The underlying method and the tool based on it [9] needs to be empirically evaluated. This is underway using the Goal-Question-Metric paradigm of Basili, et al [2]. Naturally, we are also addressing questions of scale, to determine if existing software systems decompose sufficiently via these techniques, in order to effect a technology transfer. We are also evaluating decomposition slices as candidates for components in a reuse library.

Although they seem to do well in practice, the slicing algorithms have relatively bad worst case running times, $O(n e \log(e))$, where *n* is the number of variables and *e* is the number of edges in the flowgragh. To obtain an the slices, this running time becomes $O(n^2 \epsilon \log(\epsilon))$. These worst case times would seem to make an interactive slicer for large (i.e., real) programs impractical. This difficulty can be assuaged by making the data flow analysis one component of the deliverable products that are handed off from the development team to the maintenance team. An interactive tool could then be built using these products. Then as changes are made by the maintainers the data flow data can be updated, using the incremental techniques of Keables $[17]$.

Interprocedural slices can be attacked using the techniques in Weiser [36] and Barth [1]. The interprocedural slicing algorithms of Horwitz, et al. [16] cannot be used since they require that the slice be taken at a point where the slice variable id defed or refed; we require that all slices be taken at the last statement of the program. For separate compilation, worst case assumption must be made about the external variables, if the source is not available. If the source is available, one proceeds as with procedures.

Berzins [4] has attacked the problem of software merges for *extensions* of programs. To quote him:

An extension extends the domain of the partial function without altering any of the initially defined values, while a modification redefines values that were defined initially.

We have addressed the modification problem by first *restricting* the the domain of the partial function to the slice complement, modifying the function on the values defined by the independent variables in the slice,

Figure 19: A Software Maintenance Process Model

Figure 20: A New Software Maintenance Process Model

then merging these two disjoint domains.

Horwitz, et al. [15] have addressed the modication problem. They start with a base program and two modifications it, A and B :

Whenever the changes made to base to create A and B do not "interfere" (in a sense defined in the paper), the algorithm produces a program M that integrates A and B . The algorithm is predicated on the assumption that differences in the *behavior* of the variant programs from that of base, rather than the differences in text, are significant and must be preserved in M .

Horwitz, et al. do not restrict the changes that can be made to base; thus their algorithm produces an approximation to the undecidable problem of determining whether or not the behaviors interfere. We have side-stepped this unsolvable problem by constraining the modifications that are made. Our technique is more akin to the limits placed on software maintainers. Changes must be done in a context: independence and dependence provides the context. It is interesting to note, however, that their work uses program slicing to determine potential interferences in the merge.

They do note that program variants, as they name them, are easily embedded in change control system, such as RCS [31]. Moreover, the direct sum nature of the components can be exploited to build related families of software. That is, components can be "summed" as long as their dependent code sections match exactly and there is no intersection of the independent domains. We also follow this approach for component construction.

Weiser [34] discusses some slice-based metrics. *Overlap* is a measure of how many statements in a slice are found only in that slice, measured as a mean ratio of non-unique to unique statements in each slice. Parallelism is the number of slices which have few statements in common, computed as number of slices which have pairwise overlap below a certain threshold. Tightness is the number of statements in every slice, expressed as a ratio over program length. Programs with high overlap and parallelism, but with low tightness would decompose nicely: the lattice would not get too deep or too tangled.

We have shown how a data flow technique, program slicing, can be used to form a decomposition for software systems. The decomposition yields a method for maintainers to use. The maintainer is able to modify existing code cleanly, in the sense that the changes can be assured to be completely contained in the modules under consideration and that no unseen linkages with the modified code is infecting other modules.

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